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ON FINITE FORM OF ANDREW'S IDENTITY FOR BASIS PARTITION POLYNOMIAL AND GENERALIZATION

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Abstract: Andrews gave a common generalization of the Rogers-Ramanujan series and the generating function for basis partitions. In this paper, we obtain a finite form and further generalization of this identity. As applications, some interesting identities are given.

Keywords and Phrases: BsP-polynomial, Bailey pair, Carlitz inversion, Rogers-Ramanujan identities, partition.

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1. Introduction

Basis partitions are defined as successive ranks [6] or the "rank vector" of a partition and they were first considered by Gupta [10]. More precisely, an integer partition of n is a basis partition if, in the set of all partitions of n with a given rank vector, its weight is minimum.

A partition π of a positive integer n is a finite non-increasing sequence of positive integers $(\pi_1, \pi_2, \dots, \pi_l)$ such that $n = \pi_1 + \pi_2 + \dots + \pi_l$. We write $\pi = (\pi_1, \pi_2, \dots, \pi_l)$